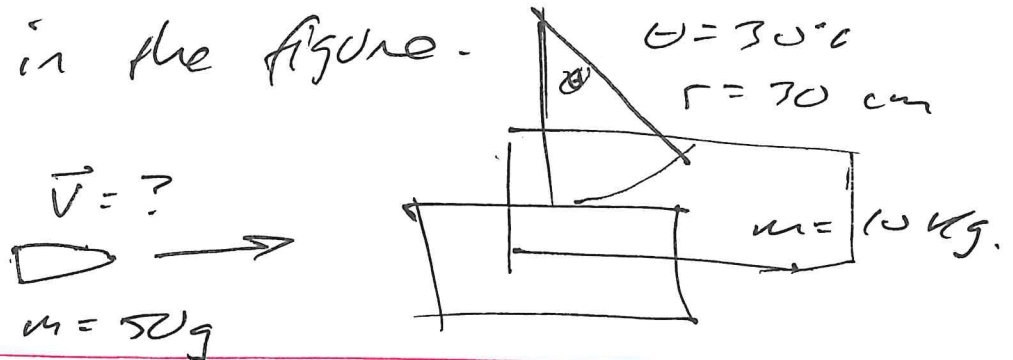


# Ballistic Pendulum Problem

A bullet is fired into a ballistic pendulum as shown in the figure.



Determine the velocity of the bullet before impact.

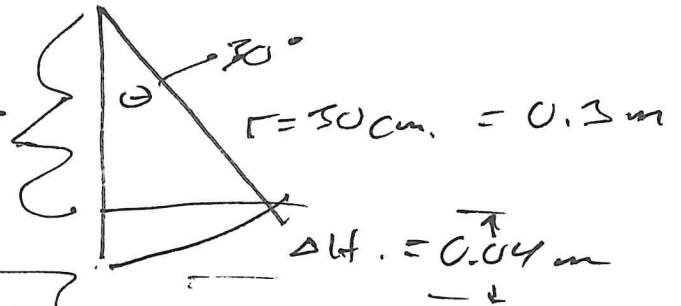
→ observation: the string holding the block of wood swings through an ~~arc~~ arc of  $30^\circ$ .

$$\textcircled{1} \text{ Use } (r = 30 \times 30\text{cm}) = 0.9\text{m}$$

$$= 0.26\text{m}$$

~~$$r = 0.3\text{m}$$~~

~~$$\Delta H = 0.3 - 0.26\text{m} = 0.04\text{m}$$~~



$$\textcircled{2} \Delta PE = m g \Delta H$$

note:  $m = \text{mass of bullet} + \text{mass of block}$   
 $= 10.05\text{kg}$

$$\text{So } \Delta PE = m \cdot g \cdot \Delta H$$

$$\Delta PE = (10.05)(9.8)(0.04) = 3.92\text{Joules}$$

③ note: the  $\Delta PE = 3.92 \text{ joules} =$  the kinetic energy  
the system must have had immediately after impact.

then here:  $KE$  (at bottom) =  $\Delta PE$  at top of arc

$$\text{so } \dots KE = \frac{1}{2} m v^2 = \Delta PE$$

$$\frac{1}{2} (10.05 \text{ kg}) (v^2) = 3.92 \text{ J}$$

★ this is the velocity of  
the system right after impact.  $\therefore v = 0.883 \text{ m/sec}$

now we use conservation of momentum to determine  
velocity of bullet before it struck the block.

$$m_1 v_1 + m_2 v_2 = (m_1 + m_2) v_f$$

bullet  $\uparrow$       block  $\downarrow$  (rest)      bullet in block

$$(0.05 \times v_1) + 0 = (10.05 \times 0.883 \text{ m/sec})$$

$$\therefore v_1 = 177 \text{ m/sec} \approx 370 \text{ mph.}$$

velocity of bullet before impact!